# Quantitative Problems in Anesthesia

David R. Moss, MD Tufts Medical Center Boston, MA

#### 1 Don't cry over spilt sevoflurane

While setting up the OR you accidentally drop a 250 mL bottle of sevoflurane. It shatters when it hits the ground.

1. Assuming the OR is a sealed container of dimensions  $25 \cdot 20 \cdot 10$  ft, what is the steady-state concentration,  $c_{ss}$  of sevoflurane in the room (in ppm)?

Room temperature is  $25^{\circ}$ C, the density of sevoflurane is 1.52 g/mL and its molecular weight is 200.

2. If the ventilation system is on and operating at the industry-standard flow rate of 15 room volume exchanges per hour, how long will it take before the concentration in the room falls below 2 ppm, the OSHA ceiling on occupational exposure to volatile anesthetics?

3. What is the initial rate of change in concentration (in ppm/min)?

# 2 Fun with E-cylinders

If a full  $O_2$  E cylinder (1900 psi) contains 660 L of  $O_2$  at STP, what is the radius of the cylinder in terms of its height, r(h) ?

### **3** IV infusion kinetics

An intravenous infusion of a drug with concentration  $c_d$  mg/ml is started with a syringe pump. The infusion line is piggybacked to a continuously dripping carrier fluid with a three-way stopcock. The distance between the stopcock and the tip of the IV catheter is the dead volume, V. The carrier flows at a rate  $Q_c$  ml/min and the drug is infused at a rate  $Q_d$ .<sup>1</sup>

1. What is the steady-state drug concentration  $c_{ss}$  at the tip of the catheter?

2. If the drug traverses V with a discrete 'head' (*Plug-Flow*), how long does it take for the drug to reach the patient's bloodstream?

3. If the drug mixes uniformly within V at all times (*Well-Mixed*), how long does it take for the drug concentration to reach 95% of steady-state?

### 4 I smell sevo!

An anesthesia delivery system at steady-state is delivering 8% sevoflurane with a total fresh gas flow Q. Prior to intubation, the mask is taken off the patient and exposed to the environment. Let V be the dead volume of the breathing system (includes the breathing circuit, breathing bag, and internal plumbing distal to the vaporizer).

1. How much wasted sevoflurane gas, W, is delivered into the OR environment in t minutes?

2. As you take off the mask you turn the sevoflurane vaporizer off. Now how much sevoflurane gas, W, is delivered into the OR environment in t minutes?

3. Now, instead of turning off the vaporizer, you turn off the fresh gas flow. How much sevoflurane gas, W, is delivered into the OR environment in t minutes?

# 5 Anesthesia at high altitude

You take an anesthesia machine up to 10,000 ft ( $P_{atm} = 500 \text{ mmHg}$ ) and set the vaporizer (calibrated at sea level) to deliver 2.1% sevoflurane (vapor pressure 160 mm). What concentration of sevoflurane gets delivered? What is the relative potency?

<sup>&</sup>lt;sup>1</sup>Adapted from Lovich et al, The Impact of Carrier Flow Rate and Infusion Set Dead-Volume on the Dynamics of Intravenous Drug Delivery. *Anesth Analg* 2005;100:1048-55.